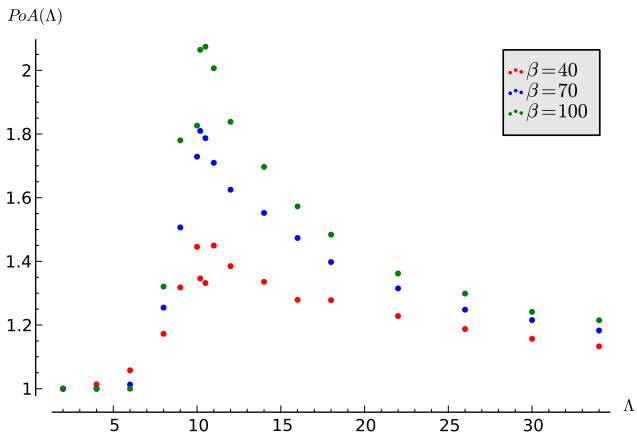


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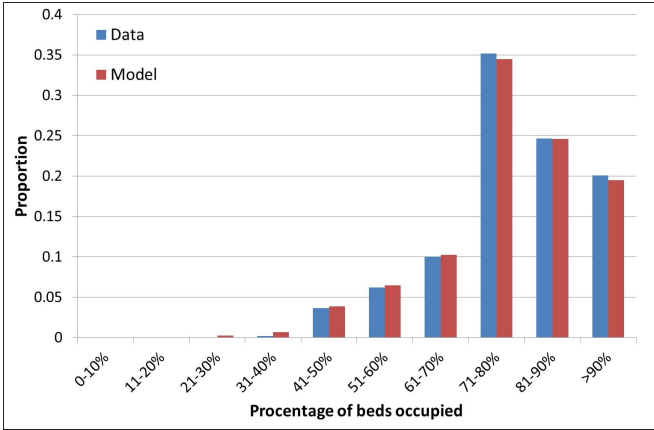
$$\begin{pmatrix} (2, 2) & (5, 0) \\ (0, 5) & (4, 4) \end{pmatrix}$$

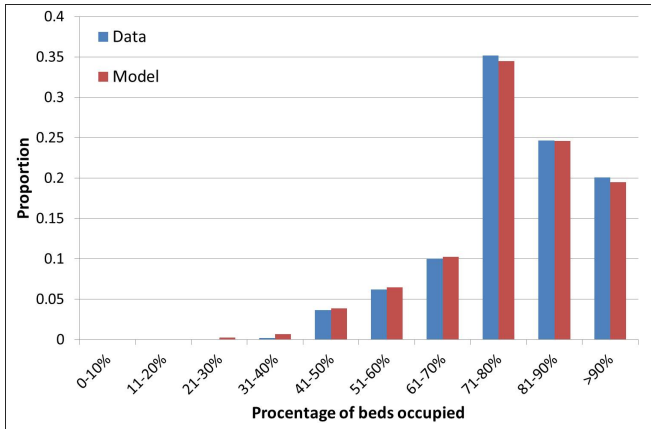


What about the controllers?

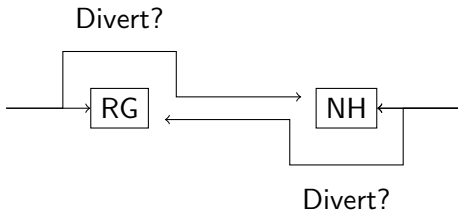
What about the controllers?

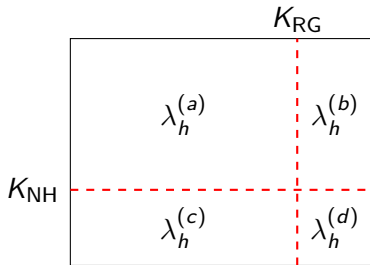
S. Deo and I. Gurvich. **Centralized vs. Decentralized Ambulance Diversion: A Network Perspective.** *Management Science*, 57(7):13001319, May 2011.

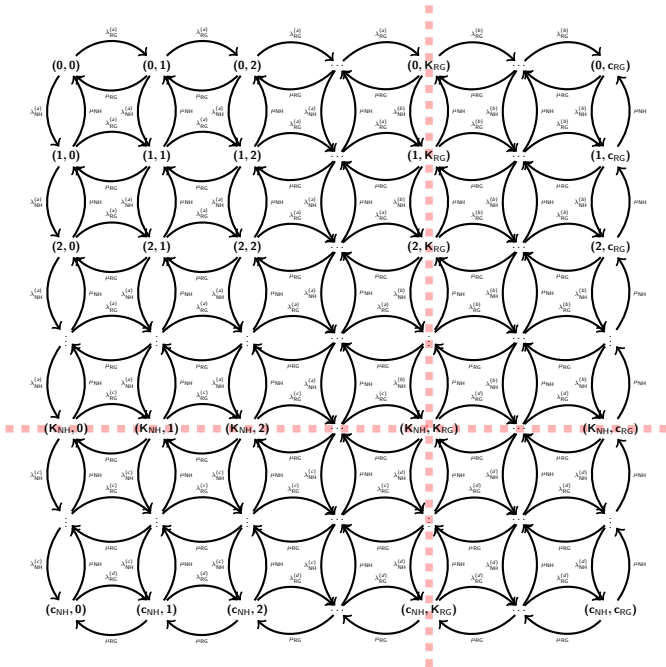


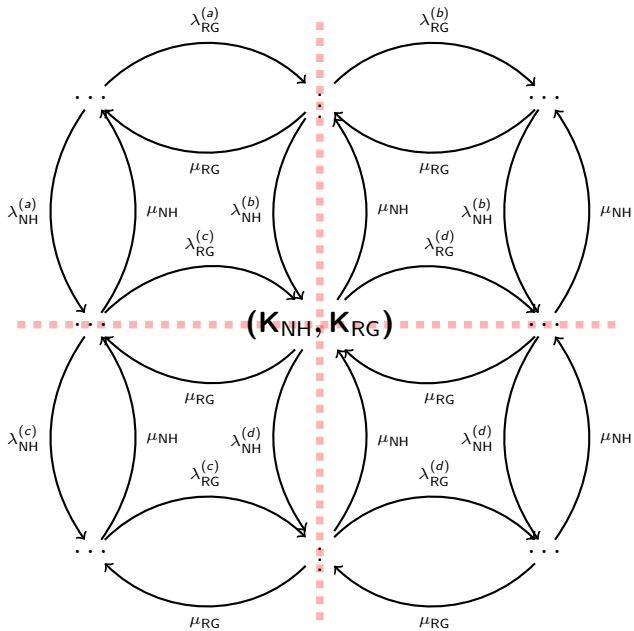


Mathematical modelling of patient flows to predict critical care capacity required following the merger of two District General Hospitals into one., *Submitted to Anaesthesia*

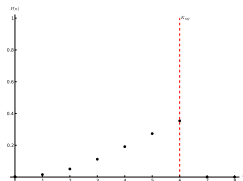




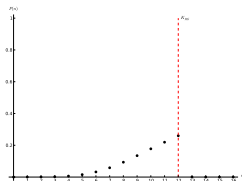




$$(K_{NH}, K_{RG}) = (6, 12):$$

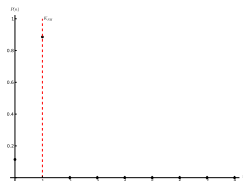


$h = NH$

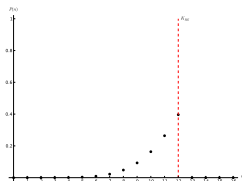


$h = RG$

$$(K_{NH}, K_{RG}) = (1, 12):$$



$h = NH$



$h = RG$

For all $h \in \{\text{NH}, \text{RG}\}$ minimise:

$$(U_h - t)^2$$

Subject to:

$$0 \leq K_h \leq c_h$$

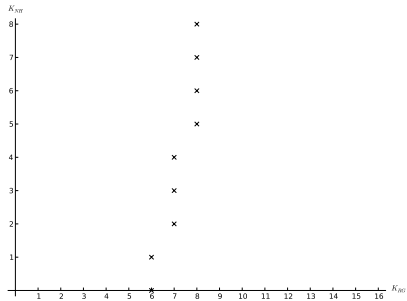
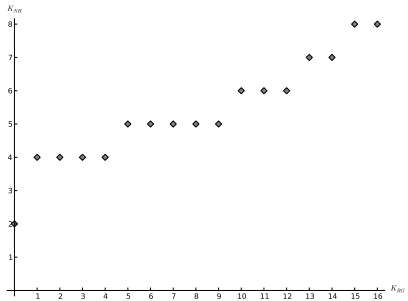
$$K_h \in \mathbb{Z}$$

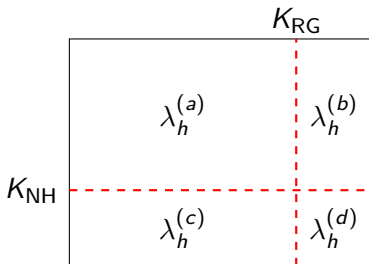
$$A = \begin{pmatrix} (U_{NH}(1, 1) - t)^2 & \dots & (U_{NH}(1, c_{RG}) - t)^2 \\ (U_{NH}(2, 1) - t)^2 & \dots & (U_{NH}(2, c_{RG}) - t)^2 \\ \vdots & \ddots & \vdots \\ (U_{NH}(c_{NH}, 1) - t)^2 & \dots & (U_{NH}(c_{NH}, c_{RG}) - t)^2 \end{pmatrix}$$

$$B = \begin{pmatrix} (U_{RG}(1, 1) - t)^2 & \dots & (U_{RG}(1, c_{RG}) - t)^2 \\ (U_{RG}(2, 1) - t)^2 & \dots & (U_{RG}(2, c_{RG}) - t)^2 \\ \vdots & \ddots & \vdots \\ (U_{RG}(c_{RG}, 1) - t)^2 & \dots & (U_{RG}(c_{RG}, c_{RG}) - t)^2 \end{pmatrix}$$

Theorem.

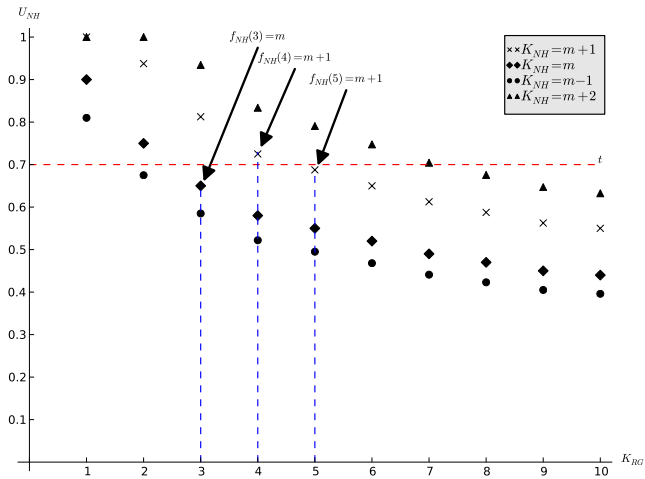
Let $f_h(k) : [1, c_{\bar{h}}] \rightarrow [1, c_h]$ be the best response of player $h \in \{\text{NH}, \text{RG}\}$ to the diversion threshold of $\bar{h} \neq h$ ($\bar{h} \in \{\text{NH}, \text{RG}\}$). If $f_h(k)$ is a non-decreasing function in k then the game has at least one Nash Equilibrium in Pure Strategies.

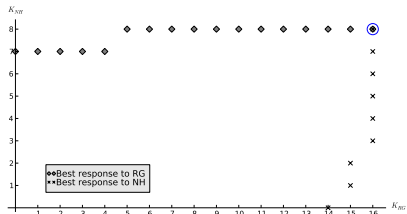




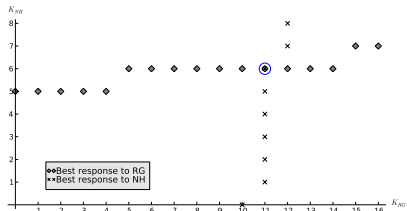
Lemma.

- ▶ If $\lambda_{NH}^{(a)} \leq \lambda_{NH}^{(b)}$ and $\lambda_{NH}^{(c)} \leq \lambda_{NH}^{(d)}$ then $f_{NH}(k)$ is a non-decreasing function in k .
- ▶ If $\lambda_{RG}^{(a)} \leq \lambda_{RG}^{(c)}$ and $\lambda_{RG}^{(b)} \leq \lambda_{RG}^{(d)}$ then $f_{RG}(k)$ is a non-decreasing function in k .



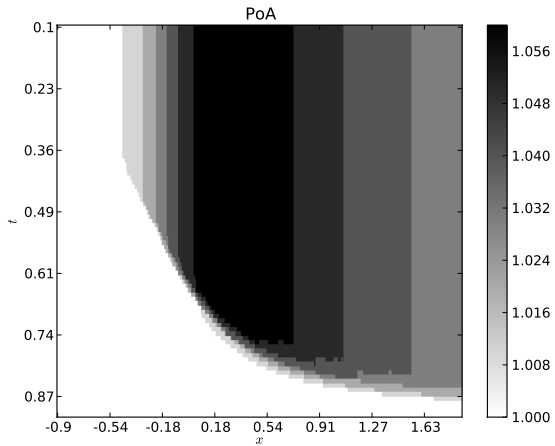


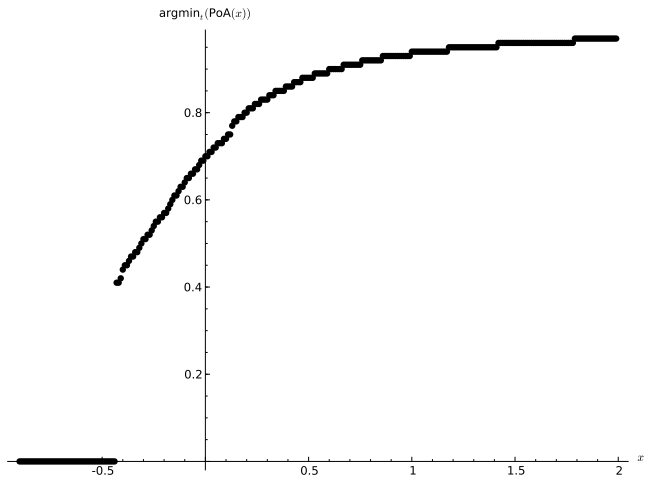
$(t = 0.8)$



$(t = 0.6)$

$$\text{PoA} = \frac{T^*}{\widetilde{T}}$$





Conclusions

- ▶ Developed a strategic form game representation of CCU interaction;
- ▶ Proved structural properties of equilibrium behaviour;
- ▶ Identified a potential justified approach to obtaining policies.

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Measuring the Price of Anarchy in Critical Care Unit Interactions, *Submitted to OMEGA*

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